



# TRANSMISSION LINE PARAMETERS

- Parameters in the transmission line
  - resistance  $r$ , inductance  $L$ , capacitance  $C$
  - $L$  and  $C$  are due to the effects of magnetic and electric fields around the conductor
- Overhead transmission line
  - ANSI voltage standard: 69kV, 115kV, 138kV, 161kV, 230kV, 345kV, 500kV, 765kV line-to-line
  - extra-high-voltage (EHV): >230kV, ultra-high-voltage (UHV):  $\geq 765\text{kV}$
  - bundling: use more than one conductor per phase, usually used at voltage > 230kV
  - advantage of bundling: increase effective radius of line conductor, reduce electric field strength and reduces corona power loss, audio loss and radio interference, and reduces line reactance



# LINE RESISTANCE

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## ■ Transmission line resistance

- **dc** flow: resistance of solid round conductor is given by  $R_{dc} = \rho l / A$
- **ac** flow: the current distribution is not uniform, the current density is **greatest at surface** of the conductor, this is called **skin effect**, therefore,  $R_{ac} > R_{dc}$
- temperature: resistance increases when temperature increases

## ■ Transmission line inductance

- definition of inductance  $L$ :  $L = \lambda / I$ ,  $\lambda$  is flux linkage
- **magnetic field density**:  $H_x = I_x / 2\pi x$ ,  $x$  is the radius of circle,  $I_x$  induces magnetic field density  $H_x$

# INTERNAL INDUCTANCE

- Derivation of internal inductance  $L_{int}$ 
  - consider the flux linked by the portion  $x \leq r$  of current  $I_a$  flowing inside a cylinder of radius  $x$ , the magnetic intensity:

$$\int H dl = I_{enclosed}$$

- Since  $I_a = \frac{\pi x^2}{\pi r^2} I$ , therefore  $2\pi x H_x = \frac{\pi x^2}{\pi r^2} I$
- magnetic flux density  $B_x$ :  
 $B_x = \mu_o H_x = \mu_o x I / 2\pi r^2$
- $\mu_o$  is the permeability of free space:  $4\pi \times 10^{-7} \text{ H/m}$
- since current flowing into the circuit of  $x$  is only a fraction of  $I_a$ , the **effective turn** is equivalent to the fraction  $N = \pi x^2 / \pi r^2$



# INTERNAL INDUCTANCE

- Derivation of internal inductance  $L_{\text{int}}$ 
  - $\pi x^2/\pi r^2$  turns of the current  $I_a$  linked by flux:
  - $$\begin{aligned} d\lambda_x &= (\pi x^2/\pi r^2) d\phi_x = (\pi x^2/\pi r^2) (B_x \times 1 dx) \\ &= (\pi x^2/\pi r^2) (\mu_o I / 2\pi r^2) \times 1 dx = (\mu_o I) x^3 / (2\pi r^4) dx \end{aligned}$$
  - total flux linkage in the inductor:
$$\lambda_{\text{int}} = \frac{\mu_o I}{2\pi r^4} \int_0^r x^3 dx = \frac{\mu_o I}{8\pi}$$
  - inductor due to the internal flux:
$$L_{\text{int}} = \mu_o / 8\pi = (1/2) \times 10^{-7} \text{ H/m}$$
  - inductor  $L_{\text{int}}$  is independent of the conductor radius  $r$

# EXTERNAL INDUCTANCE

## ■ Derivation of external inductance $L_{ext}$

- consider  $H_x$  external to conductor at  $x > r$ , since the circle at radius  $x$  enclose entire current,  $I_x = I$  ( see Fig.4.4 ):  $B_x = \mu_o H_x = \mu_o I / 2\pi x$
- the entire current  $I$  is linked by the flux outside the conductor,  $d\lambda_x = d\phi_x = B_x dx * 1 = \mu_o I / (2\pi x) * dx$
- external flux linkage between  $D_1$  and  $D_2$  :

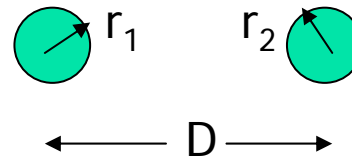
$$\lambda_{ext} = \frac{\mu_o I}{2\pi} \int_{D_1}^{D_2} \frac{1}{x} dx = 2 \times 10^{-7} I \ln \frac{D_2}{D_1} \quad \text{Wb/m}$$

- inductance between two points  $D_1$  and  $D_2$  due to the external flux:

$$L_{ext} = 2 \times 10^{-7} \ln \frac{D_2}{D_1} \quad \text{H/m}$$

# INDUCTANCE OF A SINGLE-PHASE LINE

- Single-phase line inductance in conductor 1 ( $L_1$ )
  - consider one meter length of two solid round conductors, radius  $r_1$  and  $r_2$  in the figure below:



- internal inductance:  $L_{1(int)} = (1/2) \times 10^{-7}$
- inductance beyond  $D$  links a **net current of zero** and doesn't contribute to net magnetic flux linkage, thus the external inductance  $L_{1(ext)} = 2 \times 10^{-7} \ln(D/r_1)$
- total inductance of conductor 1:

$$L_1 = L_{1(int)} + L_{1(ext)} = \frac{1}{2} \times 10^{-7} + 2 \times 10^{-7} \ln \frac{D}{r_1} = 2 \times 10^{-7} \ln \frac{1}{r_1'} + 2 \times 10^{-7} \ln \frac{D}{1}$$

where  $r_1' = r_1 e^{-\frac{1}{4}}$



# INDUCTANCE OF A SINGLE-PHASE LINE

- Single-phase line inductance

- total inductance of conductor 2:

$$L_2 = 2 \times 10^{-7} \ln \frac{1}{r_2} + 2 \times 10^{-7} \ln \frac{D}{1} \quad \text{H/m}$$

- if  $r_1 = r_2 = r$ , inductance per phase per meter length of the line:

$$L = 2 \times 10^{-7} \ln \frac{1}{r'} + 2 \times 10^{-7} \ln \frac{D}{1} \quad \text{H/m}$$

- the first term is only the fraction of conductor radius
  - the second term is dependent only on conductor spacing
  - the term  $r' = re^{-1/4}$  is called self-geometric mean distance of a circle with radius  $r$  by GMR
  - GMR is called geometric mean radius



## FLUX LINKAGE IN TERMS OF SELF AND MUTUAL INDUCTANCES

### ■ Flux linkage in a single-phase two-wire line

■ flux linkage:  $\lambda_1 = (L_{11} - L_{12})I_1$      $\lambda_2 = (-L_{21} + L_{22})I_2$

■ self and mutual inductance:

$$L_{11} = 2 \times 10^{-7} \ln \frac{1}{r_1}, \quad L_{22} = 2 \times 10^{-7} \ln \frac{1}{r_2}, \quad L_{12} = 2 \times 10^{-7} \ln \frac{1}{D}$$

■ for a group of  $n$  conductors:  $I_1 + I_2 + \dots + I_n = 0$

■ the flux linkage of conductor  $i$ :

$$\lambda_i = L_{ii}I_i + \sum_{j=1}^n L_{ij}I_j \quad j \neq i$$

$$\lambda_i = 2 \times 10^{-7} \left( I_i \ln \frac{1}{r_i} + \sum_{j=1}^n I_j \ln \frac{1}{D_{ij}} \right) \quad j \neq i$$



# INDUCTANCE OF THREE-PHASE TRANSMISSION LINES

- 3-phase line with three **symmetrical** spacing conductors, the single-phase inductance L

- **balanced** three-phase currents:  $I_a + I_b + I_c = 0$
- total flux linkage of phase a (*see fig. 4.7*):

$$\lambda_a = 2 \times 10^{-7} \left( I_a \ln \frac{1}{r'} + I_b \ln \frac{1}{D} + I_c \ln \frac{1}{D} \right)$$

- substituting for  $I_b + I_c = -I_a$ , flux linkage of phase a:

$$\lambda_a = 2 \times 10^{-7} \left( I_a \ln \frac{1}{r'} - I_a \ln \frac{1}{D} \right) = 2 \times 10^{-7} I_a \ln \frac{D}{r'}$$

- per-phase per kilo-meter length L:

$$L = 0.2 \ln \frac{D}{r'} = 0.2 \ln \frac{D}{r e^{-\frac{1}{4}}}$$
 mH/km

- inductance per-phase of a **three-phase circuit** with **equal spacing** is **the same** as one conductor of a **single-phase circuit**

# INDUCTANCE OF THREE-PHASE TRANSMISSION LINES

## ■ 3-phase line with three **asymmetrical** spacing conductors

- even in **balanced** three-phase currents, the **voltage drop** due to different line inductance will be **unbalanced**

- the phase a, b and c flux linkages:

$$\lambda_a = 2 \times 10^{-7} \left( I_a \ln \frac{1}{r'} + I_b \ln \frac{1}{D_{12}} + I_c \ln \frac{1}{D_{13}} \right)$$

$$\lambda_b = 2 \times 10^{-7} \left( I_a \ln \frac{1}{D_{12}} + I_b \ln \frac{1}{r'} + I_c \ln \frac{1}{D_{23}} \right)$$

$$\lambda_c = 2 \times 10^{-7} \left( I_a \ln \frac{1}{D_{13}} + I_b \ln \frac{1}{D_{23}} + I_c \ln \frac{1}{r'} \right)$$

- use  $\lambda = LI$

- the phase a, b, and c inductances:

$$L_a = \frac{\lambda_a}{I_a} = 2 \times 10^{-7} \left( \ln \frac{1}{r'} + a^2 \ln \frac{1}{D_{12}} + a \ln \frac{1}{D_{13}} \right)$$

$$L_b = \frac{\lambda_b}{I_b} = 2 \times 10^{-7} \left( a \ln \frac{1}{D_{12}} + \ln \frac{1}{r'} + a^2 \ln \frac{1}{D_{23}} \right)$$

$$L_c = \frac{\lambda_c}{I_c} = 2 \times 10^{-7} \left( a^2 \ln \frac{1}{D_{13}} + a \ln \frac{1}{D_{23}} + \ln \frac{1}{r'} \right)$$

- where,  $a = 1 \angle 120^\circ$ , the phase inductance contain **imaginary** term

# INDUCTANCE OF THREE-PHASE TRANSMISSION LINES

## ■ Transpose line

- practical transmission lines **cannot** maintain symmetrical spacing due to the construction considerations
- one way to **regain symmetry** and to obtain a per-phase model is to consider transposition
- transposition arrangement: **interchange phase** every **one-third** the length (*see Fig. 4.9*)
- for complete transposed lines, the inductance is the average value of  $L = (L_a + L_b + L_c)/3$
- note  $a + a^2 = 1 \angle 120^\circ + 1 \angle 240^\circ = -1$

$$L = \frac{2 \times 10^{-7}}{3} \left( 3 \ln \frac{1}{r'} - \ln \frac{1}{D_{12}} - \ln \frac{1}{D_{23}} - \ln \frac{1}{D_{13}} \right) \quad \text{H/m}$$

- rearrange equation L and we obtain ( *pp. 114-115* ):

$$L = 2 \times 10^{-7} \ln \frac{\sqrt[3]{D_{12} D_{23} D_{13}}}{r'} = 2 \times 10^{-7} \ln \frac{GMD}{GMR} \quad \text{H/m}$$

- **GMD** is geometric mean distance (equivalent conductor spacing)
- **GMR** is geometric mean radius (equivalent conductor radius)

# INDUCTANCE OF COMPOSITE CONDUCTORS

- In practical transmission line, stranded conductors and bundled conductors are used.
- The inductance of the composite conductors are analyzed with GMR and GMD
- A bundled case of single phase line with n strands in x conductor and m strands in y conductor
  - current is assumed equally divided among strands (sub-conductor), current per strand in x is  $I/n$ , current per strand in y is  $I/m$
  - flux linkage about strand a: (*from Eq. 4.43 pp.116*)

$$\lambda_a = 2 \times 10^{-7} I \ln \frac{\sqrt[m]{D_{aa} D_{ab'} \cdots D_{am}}}{\sqrt[n]{r_x' D_{ab} D_{ac} \cdots D_{an}}}$$

- inductance of strand a:

$$L_a = \frac{\lambda_a}{I/n} = 2n \times 10^{-7} \ln \frac{\sqrt[m]{D_{aa} D_{ab'} \cdots D_{am}}}{\sqrt[n]{r_x' D_{ab} D_{ac} \cdots D_{an}}}$$

■

# INDUCTANCE OF COMPOSITE CONDUCTORS

- inductance of strand n:

$$L_n = \frac{\lambda_n}{I/n} = 2n \times 10^{-7} \ln \frac{\sqrt[m]{D_{na} D_{nb'} \cdots D_{nm}}}{\sqrt[n]{r_x' D_{na} D_{nb'} \cdots D_{nc}}}$$

- average of the inductance in any strand in x

$$L_{av} = \frac{L_a + L_b + L_c + \cdots + L_n}{n}$$

- the equivalent inductance of conductor **x** in n strands

$$L_x = \frac{L_{av}}{n} = \frac{L_a + L_b + L_c + \cdots + L_n}{n^2} = 2 \times 10^{-7} \ln \frac{GMD}{GMR_x} \text{ H/m}$$

- where GMD and  $GMR_x$  are as follow:

$$GMD = \sqrt[mn]{(D_{aa'} D_{ab'} \cdots D_{am}) \cdots (D_{na'} D_{nb'} \cdots D_{nm})}$$

$$GMR_x = \sqrt[n^2]{(D_{aa} D_{ab} \cdots D_{an}) \cdots (D_{na} D_{nb} \cdots D_{nn})}$$



## GMD AND GMR OF COMPOSITE CONDUCTORS

- Definition of GMD:
  - $m$ th root of  $D$ 's product about any strand in  $x$  to strands in  $y$
- Definition of  $GMR_x$ :
  - $n$ th root of  $r_x'$  product about any strand in  $x$  to the other strands in  $x$
- GMR of the seven identical strands in a conductor
  - *see example 4.1*
  - a large number of strands in GMR calculation would be tedious, usually GMRs are available in manufacturer's data



# GMR OF BUNDLED CONDUCTORS

- Extra high voltage transmission lines are constructed with bundled conductors
- Advantages of the bundling:
  - reduce line reactance
  - increase power capability
  - reduce voltage surface gradient and corona loss
  - reduce surge impedance
- Common conductor bundling arrangement
  - two sub-conductor bundling GMR:  $D_s^b = \sqrt{D_s \times d}$
  - three sub-conductor bundling GMR:  $D_s^b = \sqrt[3]{(D_s \times d \times d)^3}$
  - four sub-conductor bundling GMR:  $D_s^b = \sqrt[4]{(D_s \times d \times d \times d \times 2^{\frac{1}{2}})^4}$



## INDUCTANCE OF THREE-PHASE DOUBLE CIRCUIT

- A three phase double circuit line consists of two identical three-phase circuits
- The circuits are operated with  $a_1$ - $a_2$ ,  $b_1$ - $b_2$ ,  $c_1$ - $c_2$  in parallel as *figure 4.13*
- Geometric arrangement of three-phase double circuit
  - unbalanced with different spacing, cause unbalanced voltage drop
  - to achieve balance, use transpose arrangement
- To obtain inductance of three-phase double circuit line, we must
  - consider transpose effect of L
  - consider bundle effect of L
  - combine transpose and bundle effects together





# INDUCTANCE OF THREE-PHASE DOUBLE CIRCUIT

## ■ Calculation of the GMD:

- starting from the calculation of per-phase GMD: group identical phase together
- find GMD between each phase group

- $$D_{AB} = \sqrt[4]{D_{a1b1}D_{a1b2}D_{a2b1}D_{a2b2}}$$

$$D_{BC} = \sqrt[4]{D_{b1c1}D_{b1c2}D_{b2c1}D_{b2c2}}$$

$$D_{AC} = \sqrt[4]{D_{a1c1}D_{a1c2}D_{a2c1}D_{a2c2}}$$

- equivalent GMD per phase is

- $$GMD = \sqrt[3]{D_{AB}D_{BC}D_{AC}}$$



# INDUCTANCE OF THREE-PHASE DOUBLE CIRCUIT

## ■ Calculation of the GMR:

- starting from the calculation of per-phase GMR:  
group identical phase together
- find GMR between each phase group

- $$D_{SA} = \sqrt[4]{(D_s^b D_{a1a2})^2} = \sqrt{D_s^b D_{a1a2}}$$

$$D_{SB} = \sqrt[4]{(D_s^b D_{b1b2})^2} = \sqrt{D_s^b D_{b1b2}}$$

$$D_{SC} = \sqrt[4]{(D_s^b D_{c1c2})^2} = \sqrt{D_s^b D_{c1c2}}$$

- where  $D_s^b$  is the two-subconductor bundled distance
- equivalent GMR per phase is  $GMR_L = \sqrt[3]{D_{SA} D_{SB} D_{SC}}$



## INDUCTANCE OF THREE-PHASE DOUBLE CIRCUIT

- The per-phase inductance of the transpose line

- $$L = 2 \times 10^{-7} \ln \frac{\sqrt[3]{D_{12} D_{23} D_{13}}}{r'} = 2 \times 10^{-7} \ln \frac{GMD}{GMR_L} \quad \text{H/m}$$

- where GMD: 
$$GMD = \sqrt[3]{D_{AB} D_{BC} D_{AC}}$$

- where GMR: 
$$GMR_L = \sqrt[3]{D_{SA} D_{SB} D_{SC}}$$

- for the inductance per-phase in mH/km

- $$L = 0.2 \ln \frac{GMD}{GMR_L} \quad \text{mH/km}$$



# REVIEW OF LINE INDUCTANCE

- Internal inductance

- $L_{\text{int}} = \mu_0 / 8\pi = (1/2) \times 10^{-7} \text{ H/m}$

- External inductance

- $L_{\text{ext}} = 2 \times 10^{-7} \ln \frac{D_2}{D_1} \text{ H/m}$

- Single-phase line inductance

- $L = 2 \times 10^{-7} \ln \frac{D}{r'} \text{ H/m}$

- Three-phase line inductance (symmetrical spacing)

- $L = 2 \times 10^{-7} \ln \frac{D}{r'} \text{ H/m}$

# REVIEW OF LINE INDUCTANCE

## ■ Three-phase line inductance (transpose line)

$$■ L = 2 \times 10^{-7} \ln \frac{\sqrt[3]{D_{12}D_{23}D_{13}}}{r'} = 2 \times 10^{-7} \ln \frac{GMD}{GMR} \quad \text{H/m}$$

## ■ Inductance of composite conductors in x group (n conductor in x, m conductor in y)

$$■ L_{av} = 2 \times 10^{-7} \ln \frac{GMD}{GMR_x} \quad \text{H/m}$$

$$■ \text{ where } GMD = \sqrt[nm]{(D_{aa'}D_{ab'} \cdots D_{am'}) \cdots (D_{na'}D_{nb'} \cdots D_{nm'})}$$

$$■ \text{ where } GMR_x = \sqrt[n^2]{(D_{aa}D_{ab} \cdots D_{an}) \cdots (D_{na}D_{nb} \cdots D_{nn})}$$

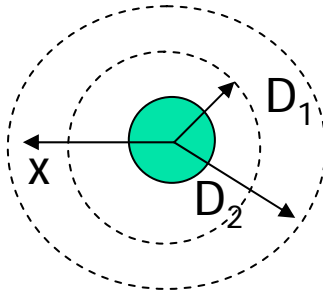
## ■ Inductance of three-phase double-circuit line (per-phase)

$$■ L = 2 \times 10^{-7} \ln \frac{\sqrt[3]{D_{AB}D_{BC}D_{CA}}}{\sqrt[3]{D_{SA}D_{SB}D_{SC}}} = 2 \times 10^{-7} \ln \frac{GMD}{GMR_L} \quad \text{H/m}$$

# LINE CAPACITANCE

## ■ Derivation of the line capacitance

- consider a long round conductor with radius  $r$  , carrying a charge of  $q$  coulombs per meter length:



- electric flux density at a cylinder of radius  $x$ :

$$D = q/A = q/(2\pi x)$$

- electric field intensity

- $E = D/\epsilon_0 = q/(2\pi\epsilon_0 x)$

- $\epsilon_0$  is the permittivity of free space:  $8.85 \times 10^{-12}$  F/m

- potential difference between cylinders from  $D_1$  to  $D_2$

- $$V_{12} = \int_{D_1}^{D_2} E dx = \int_{D_1}^{D_2} \frac{q}{2\pi\epsilon_0 x} dx = \frac{q}{2\pi\epsilon_0} \ln \frac{D_2}{D_1}$$

# CAPACITANCE OF SINGLE-PHASE LINE

## ■ Derivation of the line capacitance

- consider two conductors with radius  $r$ , carrying a charge of  $q_1$  coulombs/meter in conductor 1 and  $q_2$  in conductor 2



- voltage between conductor 1 and 2 by  $q_1$  or  $q_2$

$$V_{12(q_1)} = \frac{q_1}{2\pi\epsilon_0} \ln \frac{D}{r} \quad V_{21(q_2)} = \frac{q_2}{2\pi\epsilon_0} \ln \frac{D}{r}$$

- potential difference due to  $q_1$  and  $q_2$  ( $q_1 = -q_2$ )

$$V_{12} = V_{12(q_1)} + V_{12(q_2)} = \frac{q_1}{2\pi\epsilon_0} \ln \frac{D}{r} + \frac{q_2}{2\pi\epsilon_0} \ln \frac{r}{D} = \frac{q}{\pi\epsilon_0} \ln \frac{r}{D}$$

- capacitance between conductors

$$C_{12} = \frac{\pi\epsilon_0}{\ln \frac{D}{r}} \text{ F/m} \quad \text{or} \quad C = \frac{2\pi\epsilon_0}{\ln \frac{D}{r}} \text{ F/m}$$



# CAPACITANCE OF THREE-PHASE LINES

## ■ Derivation of the line capacitance

- consider **one meter** length of a three-phase line with three long conductors with radius  $r$ , transposed spacing shown in *figure 4.18*

- a balanced three-phase system:  $q_a + q_b + q_c = 0$

- voltage between phase a and b in **section I**

$$V_{ab(I)} = \frac{1}{2\pi\epsilon_0} \left( q_a \ln \frac{D_{12}}{r} + q_b \ln \frac{r}{D_{12}} + q_c \ln \frac{D_{23}}{D_{13}} \right)$$

- voltage between phase a and b in **section II**

$$V_{ab(II)} = \frac{1}{2\pi\epsilon_0} \left( q_a \ln \frac{D_{23}}{r} + q_b \ln \frac{r}{D_{23}} + q_c \ln \frac{D_{13}}{D_{12}} \right)$$

- voltage between phase a and b in **section III**

$$V_{ab(III)} = \frac{1}{2\pi\epsilon_0} \left( q_a \ln \frac{D_{13}}{r} + q_b \ln \frac{r}{D_{13}} + q_c \ln \frac{D_{12}}{D_{23}} \right)$$



# CAPACITANCE OF THREE-PHASE LINES

## ■ Derivation of the line capacitance (continue)

- average value of  $V_{ab}$ :

$$V_{ab} = \frac{1}{3}(V_{ab(I)} + V_{ab(II)} + V_{ab(III)}) = \frac{1}{2\pi\epsilon_0} \left( q_a \ln \frac{GMD}{r} + q_b \ln \frac{r}{GMD} \right)$$

- similarly,  $V_{ac}$ :

$$V_{ac} = \frac{1}{3}(V_{ac(I)} + V_{ac(II)} + V_{ac(III)}) = \frac{1}{2\pi\epsilon_0} \left( q_a \ln \frac{GMD}{r} + q_c \ln \frac{r}{GMD} \right)$$

- for  $q_b + q_c = -q_a$ ,  $V_{ab} + V_{ac}$ :

$$V_{ab} + V_{ac} = \frac{1}{2\pi\epsilon} \left( 2q_a \ln \frac{GMD}{r} - q_a \ln \frac{r}{GMD} \right) = \frac{3q_a}{2\pi\epsilon_0} \ln \frac{GMD}{r}$$

- for balanced three-phase voltages

- $V_{ab} + V_{ac} = 3V_{an}$  from Eq.4.83

- the capacitance per-phase to neutral

$$C = \frac{q_a}{V_{an}} = \frac{2\pi\epsilon_0}{\ln \frac{GMD}{r}} \quad \text{F/m}$$



# EFFECT OF BUNDLING

## ■ Derivation of the line capacitance (bundling)

- the effective radius of bundled conductor is  $r^b$
- the capacitor per phase for bundled conductor

$$C = \frac{2\pi\epsilon_0}{\ln \frac{GMD}{r^b}} \quad \text{F/m, where } r^b = \text{effective bundle spacing}$$

- for two-subconductor bundle :

$$r^b = \sqrt{r \times d}$$

- for three-subconductor bundle :

$$r^b = \sqrt[3]{r \times d^2}$$

- for four-subconductor bundle :

$$r^b = 1.09 \sqrt[4]{r \times d^3}$$

# CAPACITANCE OF THREE-PHASE DOUBLE-CIRCUIT LINES

## ■ Derivation of the line capacitance (three-phase)

- the effective radius of bundled conductor is  $GMR_c$
- the equivalent **per-phase capacitance to neutral**

$$C = \frac{2\pi\epsilon_0}{\ln \frac{GMD}{GMR_c}} \quad \text{F/m, where } GMR_c \text{ is for phase group}$$

- $GMR_c$  per-phase to neutral :

$$GMR_c = \sqrt[3]{r_A r_B r_C}$$

- effective radius for phase A, B, and C :

$$r_A = \sqrt{r^b D_{a1a2}}$$

$$r_B = \sqrt{r^b D_{b1b2}}$$

$$r_C = \sqrt{r^b D_{c1c2}}$$



# EFFECT OF EARTH ON THE CAPACITANCE

- The electric flux lines for an isolated charged conductor are radial and are orthogonal to cylindrical equipotential surfaces
- Earth level is like **equipotential** surface
- To simulate effect of equipotential surface, the earth level is replaced by a **fictitious charged conductor**
  - with charge equal and opposite to the charge on actual conductor
  - at a depth below the surface of the earth the same as the height of the actual conductor above earth
- The effect of the earth can **increase** capacitance
  - normally due to the height  $\gg$  distance between conductors, therefore, effect of earth is negligible
  - for balanced steady-state analysis, effect of earth is neglected
  - for unbalanced faults, earth's effect is considered



# INDUCTION

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- Magnetic field induction
  - transmission line magnetic fields affect objects close to the line
  - reason: line current produce magnetic field, magnetic field induces voltage in objects that have a long length parallel to line
- Magnetic field have been reported to affect (long term harm)
  - human blood
  - growth, behavior
  - immune systems
  - neural functions
- Electrostatic induction
  - transmission line electric fields affect objects close to the line
  - reason: high voltage produce electric field, electric field induces currents in objects in the area of the electric field
- Concern of the Electrostatic induction (instant harm)
  - human body may be exposed to steady current or spark discharge from charged objects



# CORONA

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- Corona

- the partial ionization surrounding the conductor surface
- **reason:** when surface potential gradient of a conductor exceeds the dielectric strength of the surrounding air, ionization occurs

- Corona effect

- produce power loss
- produce audible noise
- radio interference in the AM band

- Corona is affected by

- conductor diameter, bundling
- type of conductor
- condition of surface: air dust, humidity, wind

- Corona can be reduced by

- increasing the conductor size
- conductor bundling